

# Answer Set Programming in a Nutshell

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# Outline

- 1 Introduction
- 2 Foundations
- 3 Modeling
- 4 Algorithms and Systems
- 5 Potassco
- 6 Summary

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# Answer Set Programming (ASP)

- ASP is an approach to **declarative problem solving**
  - describe the problem, not how to solve it
- ASP allows for solving hard search and optimization problems
  - Systems Biology
  - Product Configuration
  - Linux Package Configuration
  - Robotics
  - Music Composition
  - ...
- All search-problems in  $NP$  (and  $NP^{NP}$ ) are expressible

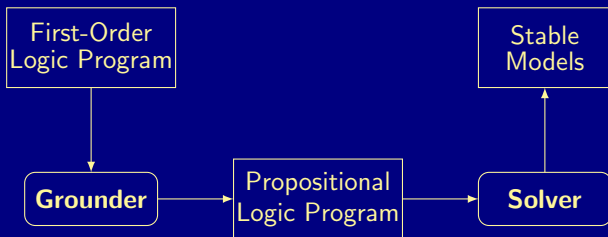
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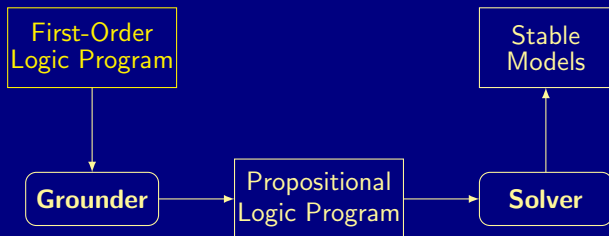
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Expressive modeling language

Powerful grounding and solving tools

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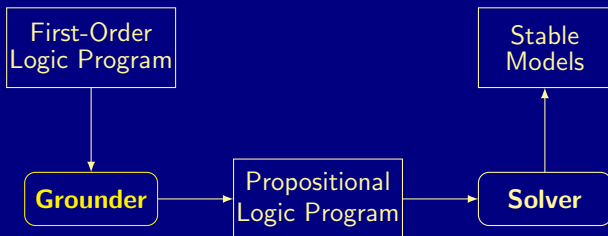


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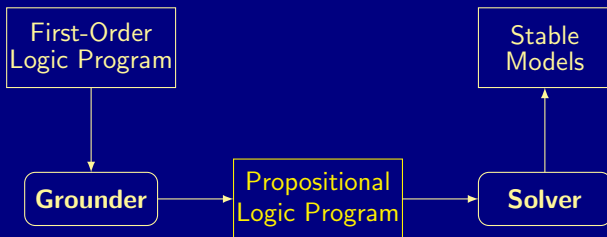
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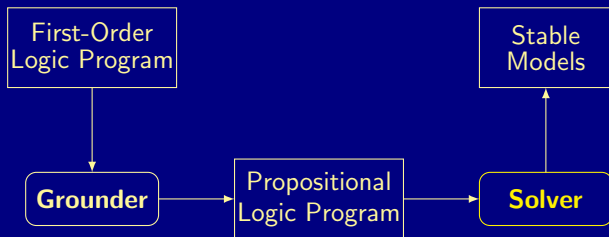
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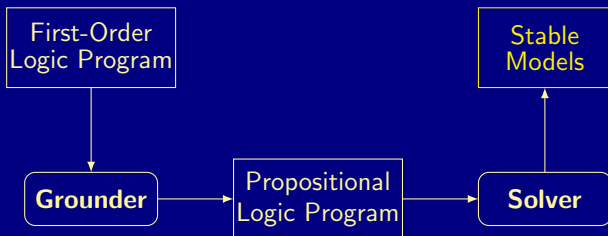
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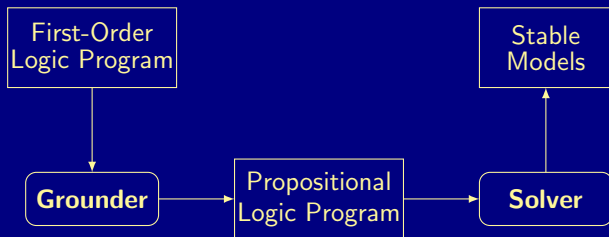
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# Propositional Normal Logic Programs

- A logic program  $\Pi$  is a set of rules of the form

$$\underbrace{a}_{\text{head}} \leftarrow \underbrace{b_1, \dots, b_m, \sim c_1, \dots, \sim c_n}_{\text{body}}$$

- $a$  and all  $b_i, c_j$  are atoms (propositional variables)
  - $\leftarrow, ,, \sim$  denote if, and, and default negation
  - intuitive reading: head must be true if body holds
- Semantics given by stable models, informally, sets  $X$  of atoms such that
  - $X$  is a (classical) model of  $\Pi$  and
  - each atom in  $X$  is justified by some rule in  $\Pi$

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# Logic Programs as Propositional Formulas

$$\Pi = \{a \leftarrow \sim b \quad b \leftarrow \sim a \quad x \leftarrow a, \sim c \quad x \leftarrow y \quad y \leftarrow x, b\}$$

$$CF(\Pi) = \{a \leftarrow \neg b \quad b \leftarrow \neg a \quad x \leftarrow (a \wedge \neg c) \vee y \quad y \leftarrow x \wedge b\} \\ \cup \{c \leftrightarrow \perp\}$$

$$LF(\Pi) = \{(x \vee y) \rightarrow a \wedge \neg c\}$$

Classical models of  $CF(\Pi)$ :

$\{b\}, \{b, c\}, \{b, x, y\}, \{b, c, x, y\}, \{a, c\}, \{a, b, c\}, \{a, x\}, \{a, c, x\},$   
 $\{a, x, y\}, \{a, c, x, y\}, \{a, b, x, y\}, \{a, b, c, x, y\}$

Unsupported atoms

Unfounded atoms

# Logic Programs as Propositional Formulas

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Classical models of  $RF(\Pi)$ : (only true atoms shown)

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- **Unfounded atoms**

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$$BF(B) = \bigwedge_{b \in B \cap atom(\Pi)} b \wedge \bigwedge_{\sim c \in B} \neg c$$

$$LF(\Pi) = \{(\bigvee_{a \in L} a) \rightarrow (\bigvee_{(a \leftarrow B) \in \Pi, B \cap L = \emptyset} BF(B)) \mid L \in loop(\Pi)\}$$

Classical models of  $CF(\Pi) \cup LF(\Pi)$ :

Theorem (Lin and Zhao)

Let  $\Pi$  be a normal logic program and  $X \subseteq atom(\Pi)$ .

Then,  $X$  is a stable model of  $\Pi$  iff  $X \models CF(\Pi) \cup LF(\Pi)$ .

- Size of  $CF(\Pi)$  is **linear** in the size of  $\Pi$
- Size of  $LF(\Pi)$  may be **exponential** in the size of  $\Pi$

## Let's run it!

```
$ cat prg.lp
```

```
a :- not b.      b :- not a.      x :- a, not c.      x :- y.      y :- x, b.
```

```
$ clingo 0 prg.lp
```

```
clingo version 4.5.0
```

```
Reading from prg.lp
```

```
Solving...
```

```
Answer: 1
```

```
a x
```

```
Answer: 2
```

```
b
```

```
SATISFIABLE
```

```
Models      : 2
```

```
Calls       : 1
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## Genuine Stable Models Semantics

- The reduct  $\phi^X$  of a formula  $\phi$  relative to a set  $X$  of atoms is defined as follows

$$\phi^X = \perp \quad \text{if } X \not\models \phi$$

$$\phi^X = \phi \quad \text{if } \phi \in X$$

$$\phi^X = (\psi^X \circ \mu^X) \quad \text{if } X \models \phi \text{ and } \phi = (\psi \circ \mu) \text{ for } \circ \in \{\wedge, \vee, \rightarrow\}$$

$$\phi^X = \top \quad \text{if } X \not\models \psi \text{ and } \phi = \sim \psi$$

Let  $\Phi$  be a formula and  $X \subseteq \text{atom}(\Phi)$ .

Then,  $X$  is a stable model of  $\Phi$  if  $X$  is a  $\subseteq$ -minimal model of  $\Phi^X$

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Definition (Gelfond and Lifschitz et al.)

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## Some language constructs

### ■ Variables

- $p(X) :- q(X)$  over constants  $\{a, b, c\}$  stands for  
 $p(a) :- q(a), p(b) :- q(b), p(c) :- q(c)$

### ■ Conditional Literals

- $p :- q(X) : r(X)$  given  $r(a), r(b), r(c)$  stands for  
 $p :- q(a), q(b), q(c)$

### ■ Disjunction

- $p(X) ; q(X) :- r(X)$

### ■ Integrity Constraints

- $:- q(X), p(X)$

### ■ Choice

- $2 \{ p(X,Y) : q(X) \} 7 :- r(Y)$

### ■ Aggregates

- $s(Y) :- r(Y), 2 \#sum \{ X : p(X,Y), q(Y) \} 7$

# Basic methodology

## Methodology

### Generate and Test (or: Guess and Check)

Generator Generate potential stable model candidates  
(typically through non-deterministic constructs)

Tester Eliminate invalid candidates  
(typically through integrity constraints)

## Peanutshell

Logic program = Data + Generator + Tester (+ Optimizer)

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# Satisfiability testing

$$(a \leftrightarrow b) \wedge c$$



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```
{ a ; b ; c }.
```

```
:- not a, b.
```

```
:- a, not b.
```

```
:- not c.
```

# Maximum satisfiability testing

$\text{"}(a \not\leftrightarrow b)\text{"} + (a \leftrightarrow b) \wedge c$

```
{ a ; b ; c }.
```

```
:- not a, b.
```

```
:- a, not b.
```

```
:- not c.
```

```
:~ a, b. [42@1]
```

```
:~ not a, not b. [69@2]
```

# n-queens

## Basic encoding

```
{ queen(1..n,1..n) }.
```

```
:- { queen(I,J) } != n.
```

```
:- queen(I,J), queen(I,JJ), J != JJ.
```

```
:- queen(I,J), queen(II,J), I != II.
```

```
:- queen(I,J), queen(II,JJ), (I,J) != (II,JJ), I-J = II-JJ.
```

```
:- queen(I,J), queen(II,JJ), (I,J) != (II,JJ), I+J = II+JJ.
```

# n-queens

## Advanced encoding

```
{ queen(I,1..n) } = 1 :- I = 1..n.  
{ queen(1..n,J) } = 1 :- J = 1..n.  
  
:- { queen(D-J,J) } >= 2, D = 2..2*n.  
:- { queen(D+J,J) } >= 2, D = 1-n..n-1.
```

## n-queens

(Experimental) constraint encoding

```
1 $<= $queen(1..n) $<= n.  
  
#disjoint { X : $queen(X) $+ 0 : X=1..n }.  
#disjoint { X : $queen(X) $+ X : X=1..n }.  
#disjoint { X : $queen(X) $- X : X=1..n }.
```

# Traveling salesperson

Basic encoding (no instance)

```
1 { cycle(X,Y) : edge(X,Y) } 1 :- node(X).
1 { cycle(X,Y) : edge(X,Y) } 1 :- node(Y).

reached(X) :- X = #min { Y : node(Y) }.
reached(Y) :- cycle(X,Y), reached(X).

:- node(Y), not reached(Y).

#minimize { C,X,Y : cycle(X,Y), cost(X,Y,C) }.
```

# Company Controls

```
controls(X,Y) :-  
    #sum+ { S: owns(X,Y,S);  
           S,Z: controls(X,Z), owns(Z,Y,S) } > 50,  
    company(X), company(Y), X != Y.
```

```
company(c_1).    owns(c_1,c_2,60).  
                 owns(c_1,c_3,20).  
company(c_2).    owns(c_2,c_3,35).  
company(c_3).    owns(c_3,c_4,51).  
company(c_4).
```

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- 1 Introduction
- 2 Foundations
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# Towards Conflict-Driven ASP

- Goal Conflict-driven approach to ASP solving
- Idea View inferences as unit propagation on nogoods

- Background

A nogood expresses an inadmissible assignment

For example, given a rule  $a \leftarrow b$

$\{\mathbf{F}a, \mathbf{T}b\}$  is a nogood (stands for  $\{a \mapsto \mathbf{F}, b \mapsto \mathbf{T}\}$ )

Unit propagation on  $\{\mathbf{F}a, \mathbf{T}b\}$  infers

$\mathbf{T}a$  wrt assignment containing  $\mathbf{T}b$

$\mathbf{F}b$  wrt assignment containing  $\mathbf{F}a$

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## Nogoods from logic programs

$$\Pi = \{a \leftarrow \sim b \quad b \leftarrow \sim a \quad x \leftarrow a, \sim c \quad x \leftarrow y \quad y \leftarrow x, b\}$$

$$CF(\Pi) = \{a \leftrightarrow \neg b \quad b \leftrightarrow \neg a \quad c \leftrightarrow \perp \quad x \leftrightarrow (a \wedge \neg c) \vee y \quad y \leftrightarrow x \wedge b\}$$

$$\cup \{B_1 \leftrightarrow \neg b \quad B_2 \leftrightarrow \neg a \quad B_3 \leftrightarrow a \wedge \neg c \quad B_4 \leftrightarrow y \quad B_5 \leftrightarrow x \wedge b\}$$

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Size of  $\Delta_{\Pi}$  is linear in the size of  $\Pi$

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# Stable Models as Solutions

## Theorem

Let  $\Pi$  be a normal logic program and  $X \subseteq \text{atom}(\Pi)$ .  
 Then,  $X$  is a stable model of  $\Pi$  iff  $X = \mathbf{A}^T \cap \text{atom}(\Pi)$   
 for a (unique) solution  $\mathbf{A}$  for  $\Delta_\Pi \cup \Lambda_\Pi$ .<sup>1</sup>

## Advantages

- Stable model computation as Boolean constraint solving
- All inferences can be seen as unit propagation on nogoods
- Nogoods readily available as conflict reasons

<sup>1</sup>A total assignment  $\mathbf{A}$  is a solution for  $\Delta_\Pi \cup \Lambda_\Pi$  if  $\delta \not\subseteq \mathbf{A}$  for all  $\delta \in \Delta_\Pi \cup \Lambda_\Pi$ .

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loop
  propagate // assign deterministic consequences
if no conflict then
  if all variables assigned then return variable assignment
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  if top-level conflict then return unsatisfiable
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    analyze // analyze conflict and add conflict constraint
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# The solver clasp

- Beyond deciding (stable) model existence, clasp allows for
  - Enumeration (without solution recording)
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  - and combinations thereof
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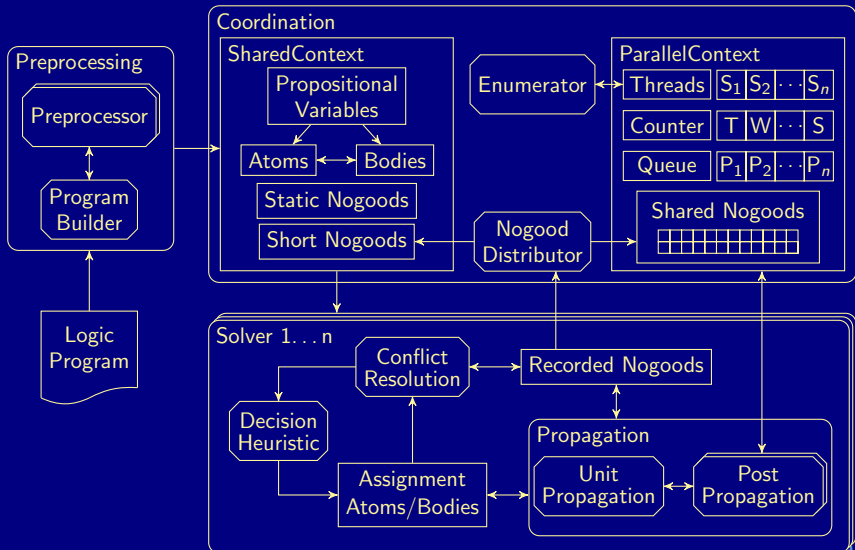
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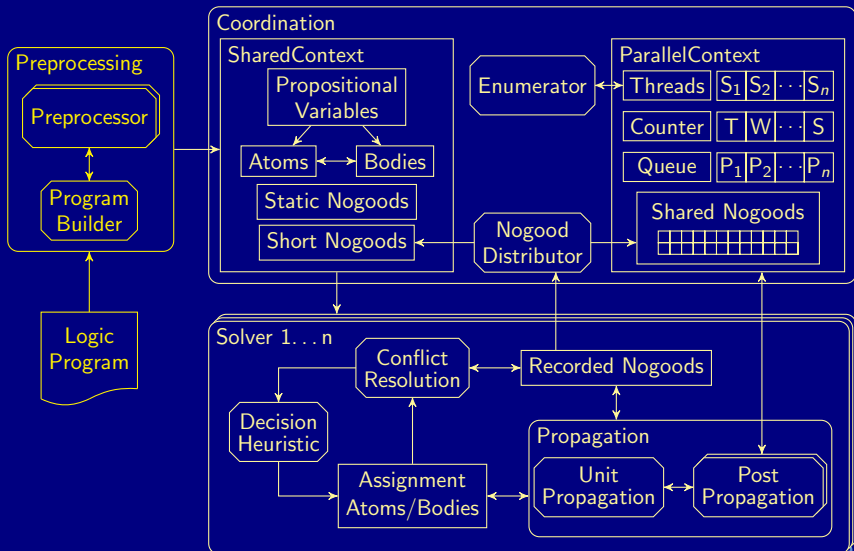
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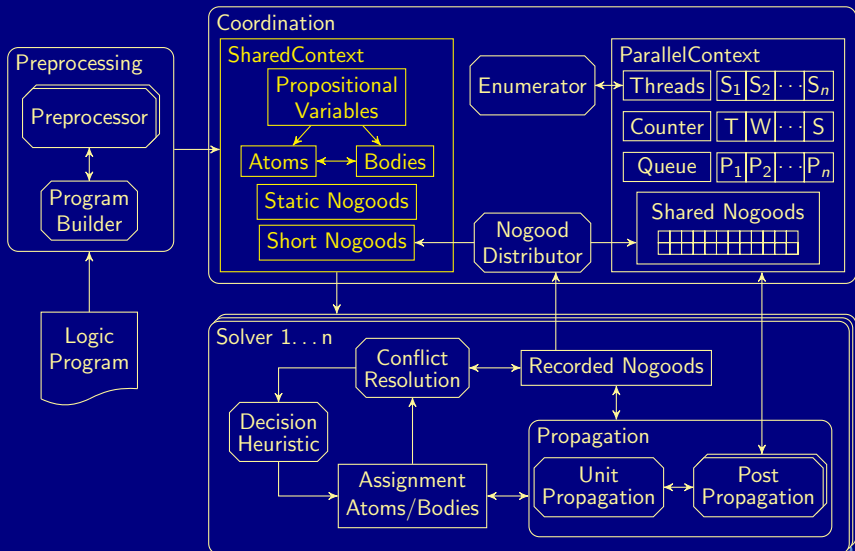
## Multi-threaded architecture of clasp



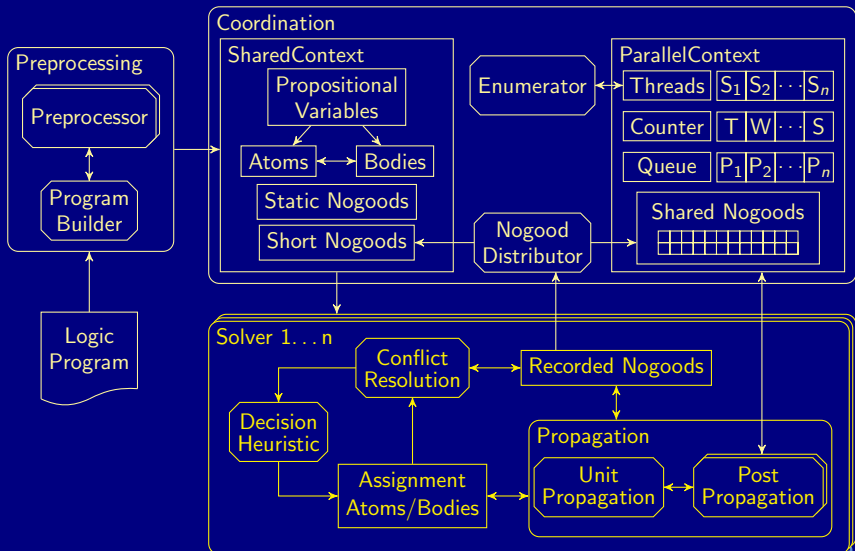
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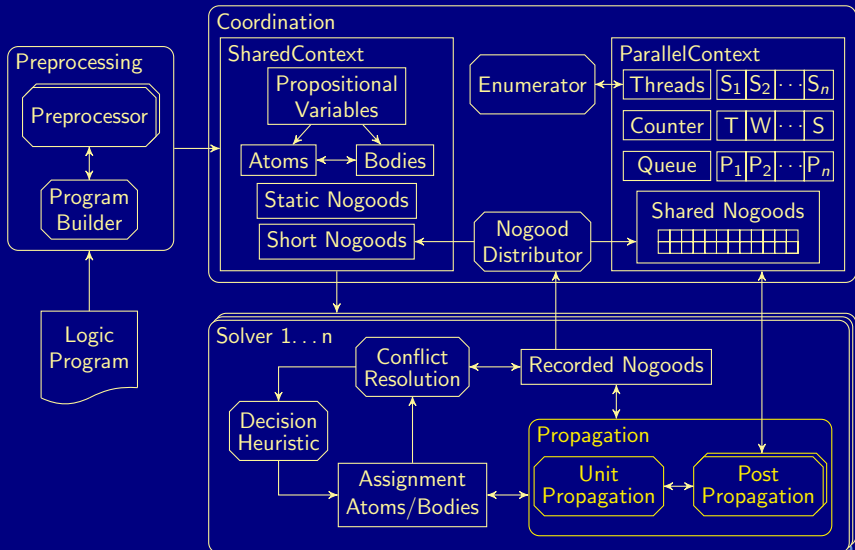
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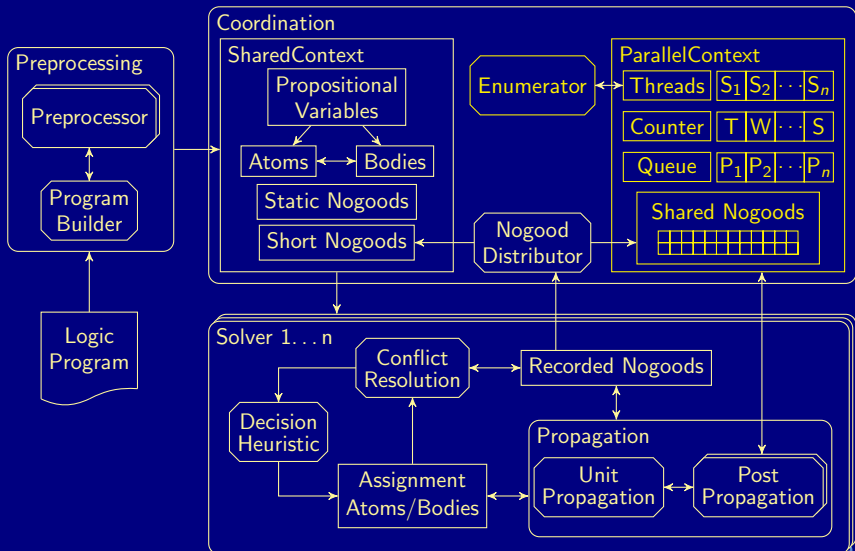


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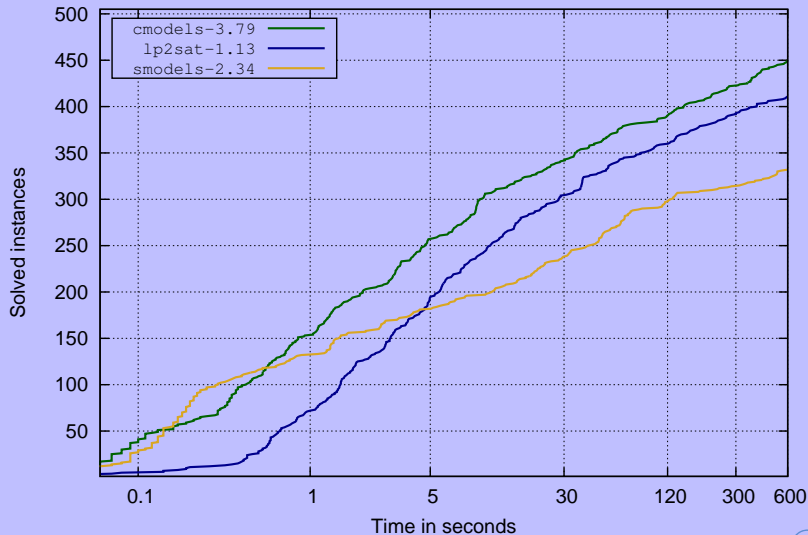


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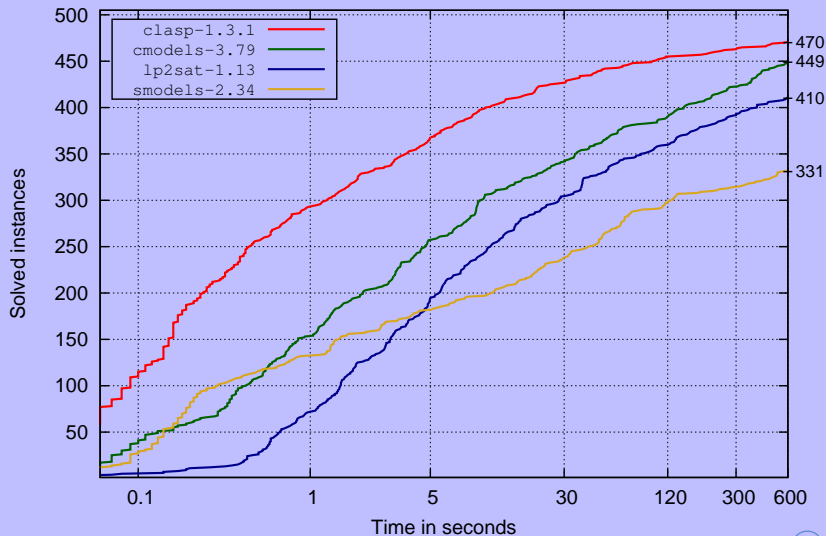
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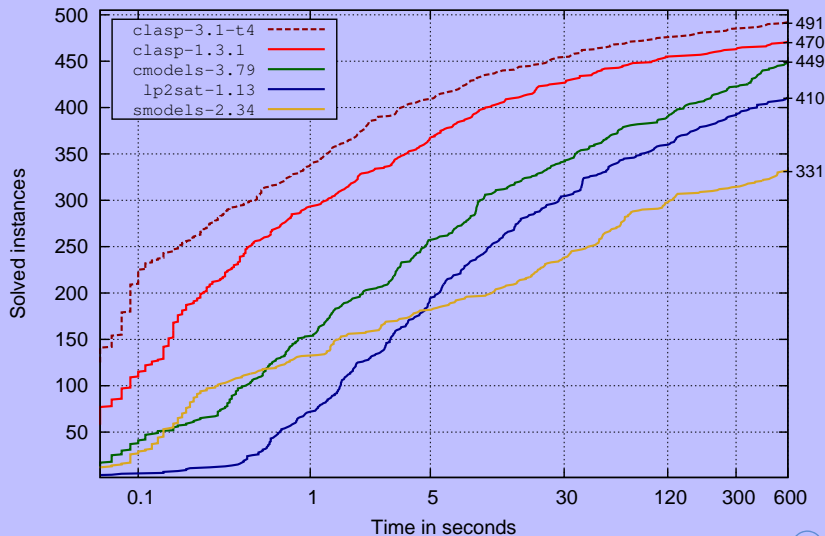
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potassco.sourceforge.net

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